

## Binomial theorem [50 marks]

1. [Maximum mark: 4] 24N.2.SL.TZ1.2  
Find the coefficient of  $x^8$  in the expansion of  $(2x - 5)^{11}$ . [4]
2. [Maximum mark: 6] 23N.1.SL.TZ1.6  
The binomial expansion of  $(1 + kx)^n$  is given by  
 $1 + \frac{9x}{2} + 15k^2x^2 + \dots + k^nx^n$ , where  $n \in \mathbb{Z}^+$  and  $k \in \mathbb{Q}$ .  
Find the value of  $n$  and the value of  $k$ . [6]
3. [Maximum mark: 7] 23M.2.SL.TZ1.6  
The coefficient of  $x^6$  in the expansion of  $(ax^3 + b)^8$  is 448.  
The coefficient of  $x^6$  in the expansion of  $(ax^3 + b)^{10}$  is 2880.  
Find the value of  $a$  and the value of  $b$ , where  $a, b > 0$ . [7]
4. [Maximum mark: 6] 22N.2.SL.TZ0.6  
Consider the expansion of  $\frac{(ax+1)^9}{21x^2}$ , where  $a \neq 0$ . The coefficient of the term in  $x^4$  is  $\frac{8}{7}a^5$ .  
Find the value of  $a$ . [6]
5. [Maximum mark: 5] 22M.1.AHL.TZ1.6  
Consider the expansion of  $(8x^3 - \frac{1}{2x})^n$  where  $n \in \mathbb{Z}^+$ . Determine all possible values of  $n$  for which the expansion has a non-zero

constant term. [5]

6. [Maximum mark: 5] 21M.1.SL.TZ2.4

In the expansion of  $(x + k)^7$ , where  $k \in \mathbb{R}$ , the coefficient of the term in  $x^5$  is 63.

Find the possible values of  $k$ . [5]

7. [Maximum mark: 5] 21M.2.SL.TZ1.6

Consider the expansion of  $(3 + x^2)^{n+1}$ , where  $n \in \mathbb{Z}^+$ .

Given that the coefficient of  $x^4$  is 20412, find the value of  $n$ . [5]

8. [Maximum mark: 6] 20N.2.SL.TZ0.S\_5

Consider the expansion of  $(3x^2 - \frac{k}{x})^9$ , where  $k > 0$ .

The coefficient of the term in  $x^6$  is 6048. Find the value of  $k$ . [6]

9. [Maximum mark: 6] 20N.2.AHL.TZ0.H\_4

Find the term independent of  $x$  in the expansion of  $\frac{1}{x^3} \left( \frac{1}{3x^2} - \frac{x}{2} \right)^9$ . [6]