

1.

[2 points]

Let the universal set U be $U = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10\}$ and let $A = \{x \mid x^2 < 20\}$, $B = \{x \mid x \text{ is a factor of } 24\}$ and $C = \{3, 4, 5\}$.

(a) State if the following are true or false and justify your answer:

(i) $B \subseteq A$

(ii) $2 \in A - B$

(iii) $(A \cup B \cup C)^c = \emptyset$

(b) Write down all elements of $B \cap C$.

2.

[2 points]

Represent the following on Venn diagrams.

(i) $(A \cap B)^c$

(ii) $(A \cup B) - C$

3.

[2 points]

Let $n(U) = 25$, $n(A) = 14$, $n(B) = 7$ and $n(A \cup B) = 18$. Represent this information on Venn diagram and find $n(A - B)$.

4.

[4 points]

In a group of 40 students:

22 like physics,

12 like chemistry,

13 like biology,

7 like physics and chemistry,

3 like physics and biology,

5 like biology and chemistry,

6 students do not like any of the three mentioned subjects.

Represent the information on a Venn diagram and find the number of students who like exactly one of the three subjects.